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Abstract

The spatial organisation of swelling clay platelets in a suspension depends on the chemical composition of the equilibration solution. Individual clay platelets can be well dispersed, with surfaces entirely in contact with the external solution, or be stacked in tactoids, where part of the surfaces forms parallel alignments embedding interlayer water and cations. External and interlayer surfaces do not exhibit similar affinities for cations having different hydration and charge properties and the clay platelet stacking arrangement influences the clay affinity for these cations. This paper aims to establish the link between exchange properties and clay tactoid size and organisation for Na-Ca exchange on montmorillonite. Different montmorillonite samples behave differently with regards to Na-Ca exchange, from ideal to non-ideal exchange behaviour. A simple model coupling the tactoid stacking size to different Na/Ca relative affinities of the external and interlayer clay surfaces enables these differences to be reproduced.

KEYWORDS: Cation exchange, montmorillonite, tactoid, stacking, compaction, model
1- Introduction

Ion exchange reactions describe the distribution of ions between adsorbed and solution phases. Such reactions have been extensively studied on clay mineral surfaces, where cations counterbalance the intrinsic negative surface charge of these materials. Cation exchange reactions involve major cations from the electrolyte background as well as trace elements in solution. Consequently, cation exchange reactions have for a long time been recognized as of great interest in many fields of investigation. Cation exchange is one of the main factors governing plant nutrient availability, such as potassium in agricultural soils [1-4]. Cation exchange reactions also explain part of the retention properties of clay minerals towards inorganic or organic compounds: heavy metals [5], radionuclides (for instance caesium, [6, 7]), antibiotics in agricultural soils [8, 9], dyes in industrial waste water [10] and other compounds. While clay mineral surfaces have a strong impact on the chemical behaviour of adjacent solutions, solution chemical composition exerts, in turn, a great influence on the physical properties of clay rocks, sediments and soils [11]. For instance, the accumulation of sodium cations in agricultural soils due to poor quality irrigation water is known to be responsible for the destructuration of these soils, reducing their permeability and their mechanical stability [12, 13]. On the other hand, the properties of clay liners used for waste confinement rely heavily on the preservation of their sodic nature, responsible for their low permeability and their semi-permeable membrane behavior [14-16]. These changes in physical properties are linked to the rearrangement of the spatial organisation of swelling clay platelets as a function of chemical conditions from well dispersed clay platelets, whose surfaces are entirely in contact with the external solution, to stacked platelets, where part of the surfaces forms parallel alignments embedding interlayer water and cations. Because external and interlayer surfaces do not a priori exhibit similar affinities for cations having
different hydration and charge properties, the clay platelet stacking arrangement is expected also to have an influence on the clay affinity for these cations [13, 17]. Given the considerable uncertainty that exists at present regarding the relevance of sorption models calibrated on suspension experiments for further applications in compact clay systems [18-20], it is important to elucidate the link between exchange properties and clay tactoid size and organisation. In this paper, Na-Ca exchange on montmorillonite is investigated as a case study. A reasonable model is constructed that treats adsorption on interlayer and external surfaces as distinct phenomena and satisfactorily describes available ion exchange data.

2- Experimental and theoretical background

2.1- Montmorillonite structure and surface charge
Montmorillonite is built from layers of oxygen atoms and cations (mainly Si\(^{4+}\), Al\(^{3+}\), Mg\(^{2+}\), Fe\(^{2+}\) or 3+ and H\(^+\)) in tetrahedral-octahedral-tetrahedral (TOT) coordination. The TOT layer structure has an excess of negative charge, due to Al for Si substitutions in tetrahedral layers and (Mg, Fe\(^{2+}\)) for (Al, Fe\(^{3+}\)) substitutions in octahedral layers. The chemical formula of a montmorillonite with both tetrahedral and octahedral substitution is (approximately) Na\(_{0.6}\)[Si\(_{7.8}\)Al\(_{0.2}\)]\(^{IV}\)[Al\(_{3.6}\)Mg\(_{0.4}\)]\(^{VI}\)O\(_{20}\)(OH)\(_4\) (omitting water), with molecular weight \(MW = 733\) g/mol. For a Wyoming MX80 montmorillonite fraction, Madsen [21] reported a \(MW\) of 745 g/mol. TOT layer negative charge is compensated by hydrated cations (e.g. Na\(^+\), Ca\(^{2+}\), Mg\(^{2+}\), K\(^+\)) in the vicinity of the charged surface (exchanged cations). TOT layers interact to form stacks of layers, hereafter named tactoids. Charge compensating cations can be located in interlayer space, sandwiched between two TOT layers, or on outer surfaces (Figure 1). Typical unit layer charges range from 0.5 to 0.9 per montmorillonite unit cell, equivalent to 0.8 to 1.2 mol kg\(^{-1}\). Outer \((A\text{ext})\) and interlayer \((A\text{int})\) surface area depends on the mean number of stacked TOT layers in tactoids \((n_c)\) according to:
\[ A_{\text{ext}} = \frac{A_{\text{tot}}}{n_c} \]  

Equation 1

and

\[ A_{\text{int}} = A_{\text{tot}} \left(1 - \frac{1}{n_c}\right) \]  

Equation 2

where \( A_{\text{tot}} \) is the total surface area (~750 m\(^2\) g\(^{-1}\), [21]), neglecting the contribution of terminating edge surface area (5-25 m\(^2\) g\(^{-1}\), [22-25]). The resulting net structural surface charge is \( \sigma_0 = -0.1 \) to \(-0.15\) C m\(^{-2}\) for both types of surface, corresponding to charges typically separated by 10 to 13 Å at the surface. For montmorillonite, the structural charge represents the essential part of the cation exchange capacity (CEC), the variable charge at the broken TOT layer edges accounting for 10% of the total negative surface charge at most [26, 27].

Figure 1. Montmorillonite TOT layer and tactoid structures.
2.2- *Na-Ca exchange reaction*

The exchange process is usually written in the formalism of a chemical reaction [13]. For Na-Ca exchange:

\[
\text{Ca}^{2+} + 2 \text{NaX} \rightleftharpoons \text{CaX}_2 + 2 \text{Na}^+ \quad \text{Reaction 1}
\]

where \(X^-\) denotes the negatively charged exchange sites that are fully compensated (no free charge) by the exchanged cations. The Na-Ca exchange equilibrium can be expressed as:

\[
K_{eq}^{\text{Na-Ca}} = \frac{([\text{Na}^+])^2}{([\text{NaX}]) ([\text{Ca}^{2+}])} \quad \text{Equation 3}
\]

where values in round brackets denote chemical activities. While activity terms for the solute part of the equation are easily obtained through the use of conventional solute activity coefficient computing methods (e.g. Davies, Debye-Hückel, Pitzer), the way to describe the activity of exchanged species is more problematic and there is no unifying theory to calculate exchanged species activity coefficients. The exchanger phase is frequently considered as analogous to a solid solution of two (or more) components [13, 28, 29]. In that case, activities of exchanged Na and Ca are expressed as:

\[
(CaX_2) = f_{Ca} N_{Ca} = \frac{[CaX_2]}{[CaX_2] + [NaX]} \quad \text{Equation 4}
\]

\[
(NaX) = f_{Na} N_{Na} = \frac{[NaX]}{[CaX_2] + [NaX]} \quad \text{Equation 5}
\]

where values in square brackets denote concentrations in mol/kg clay, \(N_i\) and \(f_i\) are respectively mole fractions and rational activity coefficients of the exchanged species \(i\). Introducing Equation 4 and Equation 5 into Equation 3, one obtains:
where \( K_v \) is the Vanselow exchange selectivity coefficient [30] that describes an ideal exchange \((f_i = 1)\). The selectivity coefficient can be measured with dedicated batch equilibration experiments between solution and exchanger (exchange isotherms), but the rational activity coefficients \( f_i \) cannot be directly measured. They can be calculated, together with the equilibrium constant, as a function of exchanger occupancy based on the exchange isotherms, but these coefficients, theoretically, cannot be further used for ternary or more complex exchange systems [28, 31].

In practice, cation exchange reactions are evaluated through the calculation of selectivity coefficients or exchange conditional constants whose definition varies as a function of empirical conventions. We introduce here, in addition to the Vanselow selectivity coefficient, the Gaines and Thomas coefficient \( K_{GT} \) [32]:

\[
K_{GT}^{Na\rightarrow Ca} = \frac{E_{Ca} \left(Na^+\right)^2}{E_{Na}^2 \left(Ca^{2+}\right)}
\]

Equation 7

where \( E_i \) denotes equivalent fraction of species \( i \):

\[
E_{Na} = \frac{[NaX]}{2[CaX_2]+[NaX]} \text{ and } E_{Ca} = \frac{2[CaX]}{2[CaX_2]+[NaX]}
\]

Equation 8

The GT coefficient is widely used in the literature for describing exchange reactions on montmorillonite surfaces. For homovalent exchange (Ca-Mg or Na-K), the GT coefficient is identical to the Vanselow coefficient but for heterovalent exchange such as Na-Ca exchange, \( K_{GT} \) and \( K_v \) are related through:

\[
K_{GT}^{Na\rightarrow Ca} = K_v^{Na\rightarrow Ca} \frac{N_{Na}^2 \times E_{Ca}}{E_{Na}^2 \times N_{Ca}^2} = \frac{4K_v^{Na\rightarrow Ca}}{1+E_{Na}^2}
\]

Equation 9
Equation 9 shows that if a 1:2 heterovalent exchange reaction (Na-Ca but also Na-Mg, Na-Cu, etc.) behaves like an ideal exchange reaction (constant \( K_v \)), then the \( K_{GT} \) value decreases from \( E_{Na} = 0 \) to \( E_{Na} = 1 \) by a factor of two. For instance, Sposito et al. [33] have demonstrated that Na-Cu exchange on Wyoming montmorillonite in perchlorate anionic background is well characterized by a constant Vanselow selectivity coefficient. Sposito and Mattigod [34] have also demonstrated that the apparent changes in \( K_{GT} \) for Na – Cu exchange on montmorillonite observed by Maes et al. [35] were in fact consistent with a constant Vanselow selectivity coefficient. This statement is also true for Na-Ni and Na-Cd exchange experiments performed by the same authors. However, this is not true for Na-Co and Na-Zn exchange with \( K_{GT} \) values varying by a factor of ten from \( E_{Na} = 0 \) to \( E_{Na} = 1 \) [35]. Previous studies showed that this variation could be due to the strong pH-dependant adsorption of transition metals on montmorillonite edge surface sites [36]: in that case, this variation should also be observed for Ni, Cu and Cd given the similar affinity of these transition metals for clay edge surfaces [37, 38]. Indeed, it has been frequently observed that, independently of the cation exchange scaling convention, the selectivity for divalent cations relative to Na increases with increasing occupancy of the exchanger by the divalent cations [13, 39, 40]. This behaviour has been attributed to contrasted behaviour of interlayer and external surfaces towards cation exchange [41-45] and thus to the formation and destruction of tactoids as a function of experimental conditions.

2.3- Influence of exchanged cations on tactoid formation

The mean number of sacked TOT layers in one tactoid depends on the exchanged cations. In a “zero” ionic strength solution, homoionic montmorillonite exchanged with divalent cations (Ca, Mg) tends to form tactoids with \( n_c \) values ranging from 4 to 7, while montmorillonite exchanged with monovalent cations (Li, Na, K) exhibits \( n_c \) values from 1 to 3 [46-48]. The
corresponding ratio of outer to interlayer surfaces ($A_{\text{ext}}/A_{\text{int}}$) varies accordingly (Figure 2).

Similar observations were made on Na-Ca clay suspensions in 0.2 mmol/L chloride electrolyte background [49], but $n_c$ increase started at higher $E_{\text{Na}}$ than in the “zero” ionic strength experiment. Stacking arrangement is thus not only dependent on the exchanged cations population but also on the ionic strength.

Figure 2. Effect of exchanged cations on tactoid formation in a Na/Ca montmorillonite system at “zero” ionic strength (data from [46]). Circles: change in the number of stacked TOT layers ($n_c$) as a function of the relative surface coverage by Na ($E_{\text{Na}}$). Triangles: corresponding ratio of outer to interlayer surfaces ($A_{\text{ext}}/A_{\text{int}}$).

2.4 - Distribution of cations on montmorillonite surfaces

The organisation of the solid-solution interface is different at external and interlayer surfaces. In the interlayer volume, clay structural negative charge is believed to be completely counterbalanced by exchanged cations. The confined space delimited by the clay surfaces (typically 6-10 Å, [50, 51]) does not enable the presence of a diffuse layer. On the other hand, structural negative charge at the external surface is not entirely counterbalanced by cation
sorption at the surface and part of the negative charge is screened in the diffuse layer. This partial compensation of charge can be probed by zeta potential measurements (e.g. [52, 53]). The distribution of cations on montmorillonite external surfaces cannot be probed directly by spectrometric methods but molecular dynamic computational methods have made it possible to show that Na\(^+\) and Ca\(^{2+}\) cations are distributed over a compact (or Stern) layer, with outer-sphere complexes, and the diffuse layer [54, 55]. Only a minor proportion of surface Na\(^+\) cations are engaged in inner-sphere complexes, where Na\(^+\) loses up to three of its hydration water molecules. This distribution is further assessed qualitatively by analogy with X-ray reflectivity results on K\(^+\) sorption on muscovite surfaces [56].

Figure 3. Schematic summary of the processes involved in aqueous clay-electrolyte interactions (modified after [42]). Reaction 1 is an exchange between cations in solution and cations in the compact (Stern) layer. Reaction 2 is an exchange between cations in solution
and cations in the electrostatic diffuse layer (EDL). Reaction 3 is an exchange between
cations in solution and cations in interlayer position.

According to the described scheme for cation sorption at montmorillonite interlayer and
external surfaces, at least three types of adsorbed species can be predicted (Figure 3): (i)
diffuse layer cations, (ii) Stern layer cations and (iii) interlayer cations. The quantitative
importance of these three adsorbed species in the overall measured exchanged selectivity are
expected to vary as a function of the stacking according to the relative external to interlayer
surface area (Equation 1 and Equation 2). Na and Ca sorption can be attributed to the three
adsorbed species according to:

\[
q_{Ca}^{\text{int}} = q_{Ca}^{\text{DL}} + q_{Ca}^{\text{Stern}} + q_{Ca}^{\text{int}}
\]

\[
q_{Na}^{\text{int}} = q_{Na}^{\text{DL}} + q_{Na}^{\text{Stern}} + q_{Na}^{\text{int}}
\]

where \( q \) denotes an equivalent charge (in mol/kg clay) and superscripts \( \text{int}, \text{Stern} \) and \( \text{DL} \)
refer to interlayer, Stern layer and diffuse layer respectively. An effective Vanselow
selectivity coefficient can be expressed for the diffuse layer as well as for the external surface
(taking into account the diffuse layer and the Stern layer):

\[
K_{v, Na \to Ca}^{\text{DL}} = \frac{q_{Ca}^{\text{DL}} \left(0.5 q_{Na}^{\text{DL}} + q_{Ca}^{\text{DL}}\right) \left(\text{Na}^{+}\right)^2}{2 \times q_{Na}^{\text{DL}} \left(\text{Ca}^{2+}\right)^2}
\]

\[
K_{v, Na \to Ca}^{\text{External}} = \frac{\left(q_{Ca}^{\text{Stern}} + q_{Ca}^{\text{DL}}\right) \left(0.5 q_{Na}^{\text{Stern}} + 0.5 q_{Na}^{\text{DL}}\right) \left(\text{Na}^{+}\right)^2}{2 \times \left(q_{Na}^{\text{Stern}} + q_{Na}^{\text{DL}}\right) \left(\text{Ca}^{2+}\right)^2}
\]
the terms $q_{Ca}^{DL}$ and $q_{Na}^{DL}$ as a function of ionic strength and the relative concentrations of cations in solution. According to this model, the mean concentration of a given cation in the diffuse layer ($c_{D,i}$ in mol/kg H$_2$O) is related to its concentration in the solution phase ($c_{free,i}$ in mol/kg H$_2$O), its charge ($z_i$) and a Donnan potential ($\psi_D$ in V) according to [58]:

$$c_{D,i} = c_{free,i} \exp\left(-\frac{z_i F \psi_D}{RT}\right)$$

Equation 13

5 The ions in the diffuse layer balance the charge from the surface:

$$\sum_i z_i c_{D,i} + Q_D = 0$$

Equation 14

where $Q_D$ is the surface charge compensated by the diffuse layer (mol$_c$ kg$_{H2O}$$^{-1}$).

Neglecting the contribution of anion exclusion, the contribution of Na and Ca cations in diffuse layer on cation exchange is given by:

$$q_{Ca}^{DL} = 2(c_{D,Ca} - c_{Ca}) \times \frac{V_D}{m_{clay}}$$

Equation 15

$$q_{Na}^{DL} = (c_{D,Na} - c_{Na}) \times \frac{V_D}{m_{clay}}$$

Equation 16

where $V_D$ is the considered volume of the diffuse layer (or Donnan volume, in L or kg$_{H2O}$) and $m_{clay}$ is the mass of clay (in kg).

We considered that the Donnan volume extends up to two Debye lengths from the surface because, in that case, the calculation of cation excess in the diffuse layer gives nearly identical results as with the Borkovec and Westall integral method for non-overlapping diffuse layers [59] but with much better numerical calculation efficiency and speed. We calculated accordingly the distribution of Ca and Na in the diffuse layer with PHREEQC v2.17, assuming either (i) a full compensation of the surface charge by the diffuse layer (0.13 C m$^{-2}$) or (ii) a compensation of only 50% of the surface charge (0.065 C m$^{-2}$). Figure 4 shows that Na is strongly preferred compared to Ca in the diffuse layer. If the surface charge
compensated by the diffuse layer decreases, then the “affinity” for Ca decreases also due to
the increase in surface potential.

Figure 4. Na-Ca selectivity coefficient ($K_v$) at an external montmorillonite surface according
to various hypotheses on ionic strength and Stern and diffuse layer properties. A: effect of the
diffuse layer only (no specific sorption of Na or Ca) on layer selectivity coefficient at two
background chloride concentrations. B: effect of Ca affinity ($\log K_{Ca}$) for the Stern layer on
the external surface selectivity coefficient at two background chloride concentrations (in that
case $\log K_{Na} = 0.8$).

The balance of the surface charge over the sites complexed with cations in the Stern layer and
the diffuse layer depends on the affinity of Na for the surface, $K_{Na}$ [60]:

$$\text{Ext}^- + \text{Na}^+ \rightleftharpoons \text{Ext} \cdots \text{Na} \quad \log K_{Na}$$

where Ext$^-$ denotes a sorption site at the montmorillonite external surface. The value of $K_{Na}$
cannot be obtained directly from an exchange experiment but can be related to the zeta
potential [61, 62] or calculated theoretically [63]. A large range of $K_{Na}$ values can be found in
the literature depending on the model used (e.g. Basic Stern -BS, Triple Layer Model -TLM,
Double Layer Model -DLM) and the representation of the interface between the clay surface
and the solution [60, 62, 64, 65]. For simplicity reasons, we considered the TLM parameters
from [54] (obtained from molecular dynamics calculations combined with zeta potential measurements) and translated them into a single log $K_{Na}$ DLM parameter ($\log K_{Na} \sim 0.8$).

We consider in the following that the sorption of $Ca^{2+}$ on montmorillonite surfaces occurs on the same sorption sites as $Na^+$. This representation must be seen as a simplification of the mechanisms, since cations of different nature can (i) be located at different distances from the surface [66] and (ii) have different mobilities and preferential positions with regard to siloxane cavities [67]. For Na-Ca exchange, Bourg and Sposito [55] showed that $Na^+$ and $Ca^{2+}$ outer-sphere surface complexes are located at essentially identical distances from the smectite surface.

We made use of one of the simplest approaches for surface complexation modelling on external surfaces, *i.e.* the electrostatic double layer model as described by Dzombak and Morel [68] and implemented in PHREEQC [69]. In this model, activities of adsorbed species are defined relative to the surface potential of the adsorption plane and surface species occupancy fraction (mole fraction in mol/total moles of sites). This choice aims at having a minimum number of parameters: only the affinity of $Ca$ for the external surface sites, $K_{Ca}$, must be fixed:

\[
2 \ Ext^- + Ca^{2+} \rightleftharpoons Ext_2 \cdots Ca
\]

log $K_{Ca}$

Reaction 3

Reaction 3 differs from the reaction described in Dzombak and Hudson [57] where $Ca^{2+}$ was assumed to interact with only a single site ($Ext^- + Ca^{2+} \rightarrow Ext \cdots Ca^+$) because the mean site spacing in clays (10 to 13 Å, see section 2.1) is much greater than the ionic radius of the $Ca^{2+}$ ion (~1 Å). The distribution of charge in clay is however not homogeneous. Charges can also be clustered in some regions of the layer or randomly distributed [70, 71] favouring $Ca^{2+}$ interaction with two charged sites.
Of course, the choice of the $K_{Ca}$ value greatly influences the external surface relative affinity for Na and Ca (Figure 4B). If $K_{Ca}$ is sufficiently low ($\log K_{Ca} = 0.7$), the overall affinity of the external surface can be lower than the “affinity” of the diffuse layer for Ca. If $K_{Ca}$ is sufficiently high ($\log K_{Ca} = 2.5$), the diffuse layer has almost no impact on the computed selectivity coefficient. The decrease in $K_{v,Na\rightarrow Ca}$ with increasing Ca population on the exchanger is related to the “mole fraction in mol/total moles of sites” convention used for surface complexation models, which is similar to a Gaines and Thomas scaling convention for cation exchange. Since a Vanselow coefficient is calculated from the results of the complexation model, the constant $\log K_{Na}$ and $\log K_{Ca}$ results in a varying $K_{v,Na\rightarrow Ca}$ according to a tendency similar to Equation 9. In both cases (low and high $K_{Ca}$ values), ionic strength has a limited effect on $K_{v,Na\rightarrow Ca}$.

According to numerous authors (see discussion in [28]), sites located on interlayer and external surfaces may have unequal cation exchange selectivity, further explaining the existence of exchangeable cations de-mixing, i.e. for instance, the preference of Na$^+$ for external surfaces in a Na-Ca montmorillonite system as probed by electrokinetic measurements [72, 73]. In that case, one expects the selectivity coefficient to vary as a function of $E_{Na}$ because of the accompanying changes in $n_c$ (Figure 2). In the following, we investigate these effects with new measurements in the Na-Ca exchange system and with data available from the literature.

3- Material and Methods

3.1- Solution preparation and concentration measurements

All solutions and suspensions were prepared with Millipore Milli-Q 18 MΩ water. LiCl, NaCl, and CaCl$_2$ solutions as well as acetic acid/acetate, MES and MOPS buffers were prepared from analytical grade salts. Na, Ca and Cl concentrations were analyzed by liquid
ion chromatography (HPLC, Dionex). Na and Ca concentrations were also measured by flame atomic absorption spectrometry (Varian 220FS).

### 3.2- Clay material

The fine fraction (<2 µm) of the MX80 natural clay sample material (commercial Wyoming bentonite, reference BF100, CETCO France) was isolated by sedimentation and re-dispersed in NaCl (0.5 mol L\(^{-1}\)). It was then successively treated with 0.1 M acetic acid in 0.5 M NaCl (pH ~ 3) to remove carbonate, DCB (dithionite – citrate – bicarbonate) to remove Fe and Mn oxides and finally with 3% H\(_2\)O\(_2\), 0.5 M NaCl at 60°C to remove organic matter. Each of the preceding treatments was followed by careful washing with 0.5 M NaCl solution. Finally, the clay was washed three times with NaCl solution (0.05 mol L\(^{-1}\)) and stored in the dark at 4°C as a concentrated suspension as recommended by Duc \textit{et al.} [74].

### 3.3- Cation exchange isotherms

Na-Ca exchange isotherms were performed at total Cl concentrations ranging from 0.01 to 0.1 mol L\(^{-1}\) and solid to liquid ratios from 0.5 to 10 g L\(^{-1}\). The chloride anionic background was preferred to a perchlorate background since it better represents the natural systems studied in our laboratory. The same method as described in Tournassat \textit{et al.} [39] was used to perform exchange isotherms. Equilibration times ranged from 24 to 60 hours, the longer times occurring when the exchange experiments were carried out over a weekend.

The amounts of exchanged Na and Ca were calculated with the following formulas:

\[
q_{Ca^{2+}} = 2 \times \frac{C_{Ca^{2+}}^{sol} \times (V_{extr} + V_{slurry}) - C_{Ca^{2+}}^{sol} \times V_{slurry}}{m_{clay}} \quad \text{Equation 17}
\]

\[
q_{Na^+} = \frac{C_{Na^+}^{sol} \times (V_{extr} + V_{slurry}) - C_{Na^+}^{sol} \times V_{slurry}}{m_{clay}} \quad \text{Equation 18}
\]
Where $C_{extr}^i$ is the concentration of cation $i$ measured in the cobalt hexamine extracting solution (in mol L$^{-1}$, [75, 76]), $C_{sol}^i$ is the concentration of cation $i$ at equilibrium with the clay before extraction (in mol L$^{-1}$), $V_{extr}$ is the volume of extracting solution added to the slurry after centrifugation (in L), $V_{slurry}$ is the volume of water in the slurry after centrifugation (in L), and $m_{clay}$ is the mass of clay (in kg).

According to the sorption mechanism depicted in Figure 3, part of the water contained in the clay slurry participates in the hydration of sorbed Na and Ca. As a consequence, we define adsorption not as a surface excess, but as a kind of partitioning into a distinct "surface water" phase. The term $V_{slurry}$ should then be corrected from this hydration water contribution. This correction can be made either by considering that hydration water is mostly interlayer water or diffuse layer water. We considered that hydration water was mostly diffuse layer water. Accordingly, we corrected the $V_{slurry}$ term by an amount of water corresponding to a volume extending up to two Debye lengths from the clay surface (750 m$^2$ g$^{-1}$). In addition to data obtained for this study, data from [39] were also reprocessed using the same procedure.

Table 1. Experimental conditions for Na-Ca cation exchange experiments

<table>
<thead>
<tr>
<th>Series n°</th>
<th>Solid to Cl solution ratio (g/L)</th>
<th>Cl concentration (mol/L)</th>
<th>Final pH range</th>
<th>Conditioning of Na-montmorillonite</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.5</td>
<td>0.01</td>
<td>4.8-5.5</td>
<td>Suspension in NaCl</td>
</tr>
<tr>
<td>2</td>
<td>0.5</td>
<td>0.05</td>
<td>4.7-4.9</td>
<td>Suspension in NaCl</td>
</tr>
<tr>
<td>3</td>
<td>8</td>
<td>0.015</td>
<td>6.9-7.2</td>
<td>Suspension in NaCl</td>
</tr>
<tr>
<td>4</td>
<td>8</td>
<td>0.05</td>
<td>6.7-7.4</td>
<td>Suspension in NaCl</td>
</tr>
</tbody>
</table>
3.4- Uncertainties

Uncertainties were calculated similarly to Tournassat et al. [39] (See electronic annex).

3.5- Light transmission measurements

Light transmission measurements were carried out on suspensions with clay contents ranging from 0.06 to 2 g L\(^{-1}\). Na-conditioned clay was washed twice (3 hours equilibrium and centrifugation) with the solution of interest (LiCl, NaCl, CaCl\(_2\), acetic acid/acetate or MOPS buffer, or a mixture of these solutions at various concentrations). Prior to spectroscopic measurements, the clay suspension was equilibrated 24 hours with the solution of interest, dispersed mechanically and ultrasonicated (3 minutes at 47 kHz). Transmittance data of suspensions were obtained using an Agilent 8453 Spectrophotometer. Measurements were made at the wavelength 650 nm. The absorbance indexes of clay suspensions were measured over the range 200-800 nm. Relative size of tactoids of ionic form \(i\) and \(j\) \((N_i\) and \(N_j\)) in suspension were related to their refractive index \(K_i\) and \(K_j\) according to [46]:

\[
\frac{K_j}{K_i} = \frac{N_i}{N_j}
\]

Equation 19

4- Results

4.1- Light transmission measurement results
Light transmission measurements enable relative sizes of tactoids in the stacking direction to be obtained as a function of experimental conditions [46]. The light transmission measurement results (Table 2) are in close agreement with literature results [46]. Na montmorillonite suspensions in NaCl 0.01 mol L\(^{-1}\) consist almost of fully dispersed TOT layers, whereas the presence of Ca in solution promotes the stacking of TOT layers. The addition of pH buffers (acetic acid/acetate and MOPS) at a concentration of 0.001 mol L\(^{-1}\) had no marked effect on the stacking of layers.

Table 2. Tactoid sizes (relative to Li-montmorillonite) inferred from light transmission measurements in various systems. (AA = acetic acid/acetate buffer).

<table>
<thead>
<tr>
<th>System</th>
<th>Ni/N(_{Li})</th>
<th>Ni/N(_{Li})</th>
</tr>
</thead>
<tbody>
<tr>
<td>This study</td>
<td></td>
<td></td>
</tr>
<tr>
<td>MX80 + LiCl 0.01M</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>MX80 + NaCl 0.01M</td>
<td>1.2-1.3</td>
<td></td>
</tr>
<tr>
<td>Na-MX80 + water (no ionic background)</td>
<td>1.1-1.3</td>
<td>1.1-1.7*</td>
</tr>
<tr>
<td>MX80 + CaCl(_2) 0.005M</td>
<td>3.1-4.1</td>
<td>2.7-&gt;20*</td>
</tr>
<tr>
<td>MX80 + NaCl 0.01M + AA 0.001M</td>
<td>1.1-1.9</td>
<td></td>
</tr>
<tr>
<td>MX80 + NaCl 0.01M + MOPS 0.001M</td>
<td>1.4</td>
<td></td>
</tr>
<tr>
<td>MX80 + NaCl 0.01M + CaCl(<em>2) 0.0001M (E(</em>{Na}) ~0.35)</td>
<td>1.5-1.7</td>
<td></td>
</tr>
<tr>
<td>MX80 + NaCl 0.01M + CaCl(<em>2) 0.0004M (E(</em>{Na}) ~0.65)</td>
<td>1.5-2.4</td>
<td></td>
</tr>
</tbody>
</table>

* Most results obtained at “zero” concentration ionic background

4.2 Exchange isotherm results
Na-Ca cation exchange results for Cl concentration lower than 0.015 mol L\(^{-1}\) are shown in Figure 5, where \(\log_{10} K_{v}^{Na\rightarrow Ca}\) is plotted as \(E_{Na}\). No clear trend in the dependency of the cation selectivity coefficient as a function of the solid to liquid ratio from 0.5 to 8 g L\(^{-1}\) can be observed while Tertre et al. observed such an effect from 2.5 to 25 g L\(^{-1}\) [78]. For all conditions, the Na-Ca selectivity coefficient is almost constant (in the limit of data repeatability) from \(E_{Na} = 0.2\) to \(E_{Na} = 0.4-0.6\) and then decreases continuously up to \(E_{Na} = 1\) but experimental results are more scattered for \(E_{Na} > 0.6\) than for \(E_{Na} < 0.6\). The same trend is also observed for experiments performed at higher chloride concentration but with selectivity coefficient values higher than those measured at low Cl concentration (Figure 6). If the GT selectivity coefficient is considered in place of Vanselow, the same trend is observed (not shown). We conclude (i) that in our experiments the solid to liquid ratio has almost no influence on the measured selectivity coefficient, (ii) that the increase in chloride background concentration causes an increase in the Na-Ca selectivity coefficient and (iii) that the changes in selectivity coefficient as a function of \(E_{Na}\) are not due to the choice of cation exchange scaling convention in the investigated systems.
Figure 5. Na-Ca exchange experiment results as a function of solid to liquid ratio for low Cl concentration ($C_{Cl} < 0.015 \text{ mol/L}$).

0 0.2 0.4 0.6 0.8 1

-0.8

-0.6

-0.4

-0.2

0

0.2

0.4

0.6

$E_{Na}$

$\log K_{Na-Ca}$

Na $\rightarrow$ Ca

0.5 g L$^{-1}$, $C_{Cl} = 0.01 \text{ mol L}^{-1}$

0.5 g L$^{-1}$, $C_{Cl} = 0.05 \text{ mol L}^{-1}$

8 g L$^{-1}$, $C_{Cl} = 0.05 \text{ mol L}^{-1}$

8 g L$^{-1}$, $C_{Cl} = 0.09 \text{ mol L}^{-1}$

Figure 6. Left: Na-Ca exchange selectivity coefficient as a function of ionic strength and solid to liquid ratio. Right: Na-Ca exchange selectivity coefficient as a function of ionic strength for $E_{Na} \sim 0.5$.

5- Discussion and modelling

5.1 Comparison with literature data

Available Na-Ca exchange data from the literature are shown in Figure 7. If possible, $K_v$ values were recalculated from tabulated solution and exchanger composition ([45, 79, 80] and [81], the latter reference giving exchange results in the system Na-Ca/Mg). In some cases, solution and exchanger phase composition were derived from exchange isotherm figures and information on the anionic salt concentration [82]. Otherwise, selectivity coefficient values were directly scanned from reference figures and if needed reprocessed as Vanselow selectivity coefficients instead of GT selectivity coefficients according to Equation 9 [43, 83-]
Error bands were not calculated due to a lack of available data for most of the experiments. Depending on the clay, the measured selectivity coefficients do not cover the same range of values. For a given clay, the measured selectivity coefficients vary by 0.5 log units from one study to the next (e.g., Upton montmorillonite). The lack of measurement reproducibility can be due, at least, to (i) different surface properties for measurements on different clays (surface charge, distribution of charges on tetrahedral and octahedral sites for instance, [86]) (ii) differences in measurement methods or natural heterogeneity of the clay samples for clay of the same origin. Despite these limitations, available literature data make it possible to distinguish at least two types of contrasting behaviour.

(i) Na-Ca exchange on Camp Berteau montmorillonite is nearly ideal in the $\text{E}_{\text{Na}}$ range 0.1-1. For $\text{E}_{\text{Na}} < 0.1$, the apparent increase in the selectivity coefficient value is not clear due to dispersion of the data.

(ii) Na-Ca exchange on Upton montmorillonite shows a tendency of selectivity coefficient decrease with increasing $\text{E}_{\text{Na}}$. This montmorillonite sample is also the only one we found that exhibits very low selectivity coefficient at $\text{E}_{\text{Na}} \sim 1$, similarly to the MX80 sample we used ($\log K_{v, Na\rightarrow Ca} < -0.8$ at $\text{E}_{\text{Na}} \sim 1$). The Wyoming Clay Spur sample also shows a tendency of selectivity coefficient decrease with increasing $\text{E}_{\text{Na}}$, although the $K_v$ variation is limited to 0.2 log units.

For Swy-1 montmorillonite, the dispersion in the results and the lack of data at $\text{E}_{\text{Na}} > 0.8$ does not make it possible to choose between these two options, ideal exchange vs. decreasing affinity for Ca as a function of Na exchanger occupancy. Baeyens and Bradbury [87] measured the distribution coefficient of Ca on Na-Swy-1 at trace concentration of Ca (i.e., $\text{E}_{\text{Na}} = 1$) with radiotracer techniques. Their distribution coefficient corresponds to a Vanselow selectivity coefficient of $0.03 \pm 0.07$ in log scale. This distribution coefficient was measured
at pH between 5 and 9 using pH buffers. The possible effect of these buffers on the TOT layer stacking was evaluated through light transmission measurements (Table 2) and we found no marked effect of their use. As a result, Na-Ca selectivity coefficient on Swy-1 at high $E_{Na}$ seems to follow a similar trend as on Camp Berteau montmorillonite, i.e. ideal exchange at high $E_{Na}$.

Figure 7. Na-Ca exchange selectivity coefficient as a function of sodium exchanger occupancy for various clays studied in the literature.

5.2- Possible sources of experimental artefact

The very low value of our selectivity coefficients at an $E_{Na}$ value close to 1 and more generally the low log $K_v$ values in the whole exchanger composition domain is unusual. According to Figure 7, such negative values in the montmorillonite Na-Ca system are very seldom reported (see [43] and, to a lesser extent, [83] for $E_{Na} < 0.6$ with no value available at higher $E_{Na}$). This statement casts some doubts on the representativeness of the data obtained.
in this study, although the repeatability of the results with regard to the results we obtained in
2009 [39] is good despite the use of a new MX80 clay stock. Sources of artefacts must then
be discussed.
Discrepancies in results could result from various causes including experimental measurement
artefacts such as incomplete recovery of exchangeable Ca\(^{2+}\) upon extraction by cobalt
hexamine or insufficient reaction time. The first hypothesis is however not realistic: (i) the
ability of the cobalt hexamine method to measure accurately cation exchange composition has
been demonstrated repeatedly [75, 76, 88, 89]; and (ii) the amount of exchanged Ca\(^{2+}\) with the
cobalt hexamine method compares well with the amount of exchanged calcium calculated
from initially added and final Ca concentration in the solution (not shown).
Insufficient experimental reaction time must also be ruled out. Na\(\rightarrow\)Ca cation exchange
reactions on montmorillonite are fast reactions [82] and our experimental equilibration time
lasted at least 24 hours, similar to the Sposito et al. study [33]. Tertre et al. showed that there
was no difference between experiments lasting three days or one week. Baeyens and
Bradbury [87] evaluated the distribution coefficient of Ca at trace concentration on Swy-1
montmorillonite and could not detect significant changes between one day and three weeks.
One other source of error could be linked to the uncertainty of the measurement at high \(E_{Na}\).
However, the extent of calculated error bands enables this hypothesis to be discarded. An
error of 1 log unit for \(K_v\) would correspond to a tenfold error on the Ca concentration or on
the amount of exchanged Ca. Both hypotheses are clearly not reasonable. As a consequence,
present evaluation of the data shows that the large changes in selectivity coefficient and its
very low minimum value are certainly not due to experimental artefacts or measurement
uncertainties. The scatter of data in some conditions must consequently be attributed to
variability in response of the system. However, discrepancies in the observed trends with
other literature data still need to be elucidated.
5.3- **Coupling tactoid formation to cation exchange mechanism**

The experimental data shown in Figure 5 were reproduced using a model combining cation exchange in interlayer and surface complexation at the external surfaces. Fitting model parameters were (i) the affinity of Ca relative to Na for the interlayer (log $K_v^{int}$ assumed constant), (ii) the affinity of Ca for the external surface (log $K_{Ca}$) and (iii) the stacking size of tactoids ($n_c$). The maximum $n_c$ value was fixed at 4.1 according to the results shown in Table 2 for the MX80 + CaCl$_2$ 0.005 mol L$^{-1}$ system. The affinity of Ca for the external surfaces (log $K_{Ca}$) was obtained from experimental points at $E_{Na} \sim 1$ where no or little stacking of clay platelet was awaited ($n_c \sim 1.1-1.2$ see Table 2). Then, the affinity of Ca for internal surfaces was obtained from data at low $E_{Na}$ with $n_c \leq 4.1$. Once these two values were obtained, data were fitted by adjusting $n_c$ for each data point. $n_c$ values at intermediate exchanger composition ($E_{Na} \sim 0.35$ and 0.65) were compared to those obtained from light transmission measurements (Table 2) and the affinities of Ca for internal and external surfaces were repetitively readjusted to better match these intermediate values. Data at higher salt concentration (Figure 6) were then fitted by adding an additional contribution from the sorption of CaCl$^+$ ion pairs on the clay external surfaces [39, 78, 90-92]. Model parameters are given in Table 3 and fitted $n_c$ values are plotted in Figure 8 and Figure 9 together with the comparison between measured and calculated selectivity coefficient values.

### Table 3. Cation exchange model parameters.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>log K</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Interlayer</strong></td>
<td></td>
</tr>
<tr>
<td>$2 \text{IntNa} + \text{Ca}^{2+} \rightleftharpoons \text{Int}_2\text{Ca} + 2 \text{Na}^+$</td>
<td>1</td>
</tr>
</tbody>
</table>
Outer surfaces

\[ \text{Ext}^- + \text{Na}^+ \rightleftharpoons \text{Ext} \cdots \text{Na} \quad 0.8 \]

\[ 2 \text{Ext}^- + \text{Ca}^{2+} \rightleftharpoons \text{Ext}_2 \cdots \text{Ca} \quad 1.2 \]

\[ \text{Ext}^- + \text{Ca}^{2+} + \text{Cl}^- \rightleftharpoons \text{Ext} \cdots \text{CaCl} \quad 2.5 \]

Figure 8. Left: comparison between experimental and model results for data at low salt concentration (open circles: system 1; closed circles: system 3; open squares: system 6; closed squares: system 7; see Table 1 for details; the straight line is the 1:1 relationship). Right: corresponding stacking number \( n_c \) as a function of Na occupancy on the exchanger. The plain lines in the right figure denote the envelope of \( n_c \) values. The gray areas are representative of \( n_c \) value deduced from light transmission measurements (Table 2).
Figure 9. Left: comparison between experimental results and model for data at high salt concentration (open circles: system 2; closed circles: system 4; open squares: system 5; see Table 1 for details; the straight line is the 1:1 relationship). Right: corresponding stacking number $n_c$ as a function of Na occupancy on the exchanger.

Experimental results (apparent log $K_v$ values) are well reproduced by the model. It can be argued, however, that the model parameter set is certainly not unique. In the proposed model (Table 2), Ca affinity for external surfaces is lower than Na affinity ($\log K_{Ca} - 2 \log K_{Na} = -0.4$). McBride [13] pointed out that montmorillonite charge sites are typically separated by 10 to 15 Å, favouring Na$^+$ as compared to Ca$^{2+}$ for electrostatic bonds at the external surfaces. Differences in structural charge distribution and location in the TOT layer of montmorillonite samples [70, 71], correlated to differences in electrostatic terms and/or configurational entropy changes [13], could be reflected in turn in the $K_{Na}$ and $K_{Ca}$ value of the present model. Ideally, these values should be obtained by measurements independent of cation exchange isotherms on various clay samples exhibiting contrasting Na-Ca exchange
behaviour. The evolution of $n_c$ as a function of $E_{Na}$ is not found to be identical to that depicted in Figure 2 but is in relative good agreement with values obtained in the present study at $E_{Na}$ ~0.35 and 0.65. According to Verburg and Baveye [77], $n_c$ values can differ significantly from one experiment to another as a function of the suspension preparation procedure and ionic strength. For instance, Lahav and Bannin [49] showed a gradual increase in the absorbance index ratio from $E_{Na} = 0$ to $E_{Na} = 0.5$ and then a sharp increase in this index ratio from $E_{Na} = 0.5$ to $E_{Na} = 0.15$ in a Na/Ca montmorillonite exchange experiment performed at 0.2 mmol/L Cl background electrolyte concentration. The important point, here, is that $n_c$ changes as a function of $E_{Na}$ are consistent with existing data: the minimum value of $n_c$ at $E_{Na}$ ~ 1 is slightly above 1, and the maximum $n_c$ value at $E_{Na}$ ~ 0 is about 4, in close agreement with measured values reported (Table 2). Moreover, the increase in $n_c$ is enhanced at an $E_{Na}$ value below 0.4, also in agreement with literature data [46, 48, 93]. As a consequence, tactoid formation upon sorption of Ca on clay surfaces can account for the observed cation selectivity changes as a function of exchanger composition.

5.4- Application to literature data

The model with parameters given in Table 3 was applied to literature data and with minimum and maximum $n_c$ values given by the envelope of values shown in Figure 8 (“minimum and maximum $n_c$”). Data from Kopittke et al. [83] are correctly reproduced by the model as a function of ionic strength. At 0.01 mol/L chloride electrolyte background, data are best reproduced using the minimum $n_c$ curve (Figure 8), while at 0.025 and 0.05 M Cl electrolyte background, data are best reproduced with $n_c$ values in-between minimum and maximum $n_c$ curves. At 0.2 M Cl, the model fails to reproduce the measured trend of selectivity coefficient variation. However, in these conditions, one expects large error bands on the experimental data (see Figure 6). The model is also in near agreement with data from Jannsen et al. [84] if
the maximum $n_c$ curve is considered. These model predictions can also be used to see how sensitive the model is to the choice of $n_c$ value: up to one order of magnitude difference is obtained in apparent $\log K_{Na\rightarrow Ca}^{v}$ when a $n_c$ value of 1 is chosen in place of a $n_c$ value of 1.3 at $E_{Na}$ value close to 1. It may also be seen that using the maximum $n_c$ curve as an input parameter enables $\log K_{Na\rightarrow Ca}^{v}$ variations accounting for less than 0.3 log units to be obtained.

![Graph showing comparison of model prediction with data from Kopitke et al. ([83], open circles) and Jannsen et al. ([84], black squares). “Maximum” and “minimum $n_c$” refer to the $n_c$ envelope curves shown in Figure 8.](image)

Data obtained on Camp Berteau montmorillonite [85, 86] with an almost constant selectivity coefficient value (~0.3) could not be predicted by the model without raising the $n_c$ values above the maximum values shown on Figure 8. A $n_c$ value of ~20 was necessary to reproduce
experimental data at low $E_{Na}$ (Figure 11). Although this value is far higher than the value obtained in the present study for MX80 montmorillonite, it is still in agreement with other values reported in the literature (Table 2, [77]). The speed of shaking and the volume of suspension per flask significantly affect the thickness and lateral extent of the quasi-crystal [77, 94]. Impurities such as adsorbed $Al^{3+}$ could also play a role by influencing the stacking arrangements of montmorillonite lamellae [90]. As a consequence, observed differences amongst published cation exchange data could be due to differences in platelet stacking during the experiments. This platelet stacking effect has already been proved for the Mg-K exchange reaction on montmorillonite where forward reaction (Mg replaced by K) and backward reaction (K replaced by Mg) did not lead to identical exchange selectivity coefficients [11]. Moreover, the selectivity coefficients evolved slowly with time and this evolution was correlated with a change in tactoid size. The present modelling study shows that this effect may also be true for Na-Ca and other monovalent-divalent exchange reactions. The main difficulty arising from this modelling analysis is the absence of a unique set of parameters reproducing the data for Na-Ca exchange on various montmorillonite samples.
Figure 11. Comparison of data from Van Bladel et al. on Camp Berteau montmorillonite ([85], circles on left figures) model (plain lines on left figures) using adjustable $n_c$ values (right figures).
5.5- Implications for cation exchange in compacted systems (clayrocks, sediment, soils)

The effect of tactoid size implies that selectivity values obtained for heterovalent cation exchange (Na-Me\(^{2+}\), where Me stands for a divalent cation) in laboratory experiments could not be directly transferable to natural systems. Natural clay systems (clayrocks, sediments or soils) exhibit textural properties that can differ from dilute suspensions: in particular, higher \(n_c\) values are expected due to compaction of the material [95]. Figure 12 shows the effect of ionic strength and compaction on the apparent Na-Ca selectivity coefficient calculated with the present model (\(n_c = 5, 10\) and 20 for illustrative purposes, [11, 96]). If parameters are taken from Table 3, then the apparent selectivity coefficient value varies from 0 to 1 as a function of compaction, ionic strength and exchanger composition.

Figure 12. Effect of stacking due to compaction (\(n_c\)) and ionic strength on the apparent Na-Ca selectivity coefficient.

Conclusions

We have shown that different montmorillonite samples behave differently with regards to Na-Ca exchange, from ideal to non-ideal exchange behaviour. Exchange data can be reproduced by a model coupling the tactoid stacking size to different Na/Ca relative affinities of the external and interlayer clay surfaces. According to this model, clays would have low affinity
for Ca on their external surfaces. This result has implications on the applicability of selectivity coefficients determined from experiments in dispersed suspension for the prediction of compacted clay-rock properties where the effect of platelet stacking should be taken into account.

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